

Magnetic dipole moment:

$$M = m \times 2\ell \quad [\text{A m}^2 \text{ or J T}^{-1}]$$

m = pole strength (A m), 2ℓ = magnetic length

Axial field ($r \gg \ell$):

$$B_{\text{axial}} = \frac{\mu_0}{4\pi} \cdot \frac{2M}{r^3} \quad (\text{direction: along } \vec{M})$$

Equatorial field ($r \gg \ell$):

$$B_{\text{equat}} = \frac{\mu_0}{4\pi} \cdot \frac{M}{r^3} \quad (\text{direction: opposite to } \vec{M})$$

Important ratio:

$$B_{\text{axial}} = 2 B_{\text{equat}} \quad (\text{at equal distances})$$

General point (angle θ from axis):

$$B = \frac{\mu_0 M}{4\pi r^3} \sqrt{3 \cos^2 \theta + 1}$$

Torque:

$$\tau = MB \sin \theta \quad (\text{max when } \theta = 90^\circ)$$

Potential energy:

$$U = -MB \cos \theta$$

- Stable equilibrium: $\theta = 0^\circ$, $U_{\text{min}} = -MB$
- Unstable equilibrium: $\theta = 180^\circ$, $U_{\text{max}} = +MB$

Work done to rotate $\theta_1 \rightarrow \theta_2$:

$$W = MB(\cos \theta_1 - \cos \theta_2)$$

Time period of vibration magnetometer:

$$T = 2\pi \sqrt{\frac{I}{MB}}$$

Comparing magnets (same I):

$$\frac{T_1}{T_2} = \sqrt{\frac{M_2}{M_1}} \Rightarrow \frac{M_1}{M_2} = \frac{T_2^2}{T_1^2}$$

Tan-A & Tan-B positions (deflection magnetometer):

$$\text{Tan-A: } M = \frac{4\pi}{\mu_0} \cdot \frac{d^3}{2} \cdot H \tan \theta$$

$$\text{Tan-B: } M = \frac{4\pi}{\mu_0} \cdot d^3 \cdot H \tan \theta$$

Magnetic moment:

$$M = NIA$$

Circular loop (radius r):

$$M = NI\pi r^2$$

Bohr Magneton (smallest unit of magnetic moment):

$$\mu_B = \frac{eh}{4\pi m_e} = 9.27 \times 10^{-24} \text{ J T}^{-1}$$

Gyromagnetic ratio:

$$\frac{M_I}{L} = \frac{e}{2m_e} \approx 8.8 \times 10^{10} \text{ C kg}^{-1}$$

Three elements (most NEET-tested topic):

| Element | Meaning |
|-----------------------------------|--|
| Magnetic Declination (δ) | Angle between true north and magnetic north (horizontal plane) |
| Angle of Dip (ϕ) | Angle between \vec{B}_E and horizontal (vertical plane) |
| Horizontal Component | $H = B_E \cos \phi$ |
| Vertical Component | $V = B_E \sin \phi$ |

Key relations:

$$B_E = \sqrt{H^2 + V^2}$$

$$\tan \phi = \frac{V}{H}$$

Special locations:

- Magnetic poles: $\phi = 90^\circ$, $H = 0$, $B_E = V$
- Magnetic equator: $\phi = 0^\circ$, $V = 0$, $B_E = H$

Apparent dip (plane rotated by α from magnetic meridian):

$$\tan \phi' = \frac{\tan \phi}{\cos \alpha}$$

Neutral points (bar magnet horizontal, N facing north):

- Neutral points: on **equatorial line**
- N facing south: neutral points on **axial line**

Magnetisation (intensity of magnetisation):

$$I = \frac{M_{\text{net}}}{V} \quad [\text{A m}^{-1}]$$

Magnetic susceptibility:

$$\chi_m = \frac{I}{H}$$

Relative permeability:

$$\mu_r = 1 + \chi_m \quad \mu = \mu_0 \mu_r$$

Magnetic flux density:

$$B = \mu_0(H + I) = \mu_0 \mu_r H$$

- **Coercivity:** H needed to make $B = 0$ (demagnetising force)
- **Hysteresis loss** \propto area enclosed by B-H loop

| Property | Perm. Magnet | Soft (Electromagnet) | Iron |
|--------------|---------------|----------------------|------|
| Retentivity | High | High | |
| Coercivity | High | Low | |
| Area of loop | Large | Small | |
| Material | Steel, Alnico | Soft Fe, Mumetal | |

Transformer core: Soft iron (low hysteresis loss).
Permanent magnet: Steel/Alnico (high coercivity).

$$\oint \vec{B} \cdot d\vec{A} = 0$$

- No magnetic monopoles exist
- Magnetic field lines are always **closed loops**
- Both inside and outside a magnet: lines are closed

| | Dia | Para | Ferro |
|-------------|---------------------|--|--------------------|
| χ_m | Small -ve | Small +ve | Large +ve |
| μ_r | < 1 | > 1 (slight) | $\gg 1$ |
| In field | Repelled | Weakly attracted | Strongly attracted |
| Temp effect | None | Decreases | Drops at T_C |
| Examples | Cu, Bi, Water, NaCl | Al, O ₂ , CuCl ₂ | Fe, Ni, Co |

Superconductors: Perfect diamagnets, $\chi_m = -1$, $\mu_r = 0$

1. **Earth's magnetism** (dip, H , V , B_E) — asked almost every year
2. **Vibration magnetometer** $T = 2\pi\sqrt{I/MB}$ — comparing magnets, sum/difference positions
3. **Properties of dia/para/ferro** — assertion-reason type
4. **Neutral points** of bar magnet — conceptual
5. **Curie's law** $\chi \propto 1/T$ — graph-based question
6. **Hysteresis** — identify material from B-H graph
7. $B_{\text{axial}} = 2B_{\text{equat}}$ at equal distance
8. **Retentivity vs Coercivity** for permanent vs soft magnet
9. **Bohr magneton** value: $9.27 \times 10^{-24} \text{ J T}^{-1}$
10. **Apparent dip formula:** $\tan \phi' = \tan \phi / \cos \alpha$

Curie's Law (paramagnetics):

$$\chi_m = \frac{C}{T} \Rightarrow \chi_m \propto \frac{1}{T}$$

Curie-Weiss Law (ferromagnetics, $T > T_C$):

$$\chi_m = \frac{C}{T - T_C}$$

Curie temperature T_C : Above T_C , ferromagnetic \rightarrow paramagnetic.

- Fe: $\approx 1043 \text{ K}$ Co: $\approx 1388 \text{ K}$ Ni: $\approx 631 \text{ K}$

Diamagnetics: Susceptibility nearly **independent of temperature**.

8. Hysteresis Loop

- **Retentivity:** B when $H = 0$ (residual magnetism)

COMMON NEET CONFUSIONS

- **Dip vs Declination:** Dip is in the *vertical* plane; declination is in the *horizontal* plane. Very commonly confused.
- **Neutral points direction:** N-pole facing geographic north \Rightarrow neutral points on equatorial line (perpendicular bisector), *not* axial line.
- **Magnetic equator vs geographic equator:** These are *different*. At magnetic equator, dip = 0; do not confuse with geographic equator.
- **Diamagnetic** $\chi_m < 0$: NEET often asks whether susceptibility is zero or negative. It is **negative**, not zero.
- **Curie law applies to paramagnetics only:** Ferromagnetics follow Curie-Weiss law above T_C .

Below T_C they are ferromagnetic.

- **Soft iron vs steel:** Soft iron has *high retentivity* but *low coercivity* — ideal for electromagnets. Steel has high coercivity — ideal for permanent magnets.
- **Direction of equatorial field:** Equatorial \vec{B} is *antiparallel* to \vec{M} . Many students draw it in the same direction as axial field.
- $T \propto 1/\sqrt{M}$ **not** $1/M$: In vibration magnetometer, $T \propto 1/\sqrt{M}$ — a common calculation error.
- **Apparent dip at $\alpha = 90^\circ$:** $\cos 90^\circ = 0 \Rightarrow \tan \phi' \rightarrow \infty \Rightarrow \phi' = 90^\circ$. This is the “dip at a plane perpendicular to meridian” result.
- **Ferromagnetic domains:** Below T_C , ferromagnets have *domains* (regions of aligned dipoles). Above T_C , domains break down \rightarrow paramagnetic behaviour.

$$\mu_0 = 4\pi \times 10^{-7} \text{ T m A}^{-1} \quad \frac{\mu_0}{4\pi} = 10^{-7} \text{ T m A}^{-1}$$

$$\mu_B = 9.27 \times 10^{-24} \text{ J T}^{-1} \quad B_E \approx 3.6 \times 10^{-5} \text{ T}$$

$$\text{Dip at poles} = 90^\circ \quad \text{Dip at equator} = 0^\circ$$